Biogeochemical modelling of anaerobic vs. aerobic methane oxidation in a meromictic crater lake (Lake Pavin, France)

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Abstract

Methane is a powerful greenhouse gas and its concentration in the atmosphere has increased over the past decades. Methane produced by methanogenic Archaea can be consumed through aerobic and anaerobic oxidation pathways. In anoxic conditions found in freshwater environments such as meromictic lakes, CH\textsubscript{4} oxidation pathways involving different terminal electron acceptors such as NO\textsubscript{3}, SO\textsubscript{4}\textsuperscript{2-}, and oxides of Fe and Mn are thermodynamically possible. In this study, a reactive transport model was developed to assess the relative significance of the different pathways of CH\textsubscript{4} consumption in the water column of Lake Pavin. In most cases, the model reproduced experimental data collected from the field from June 2006 to June 2007. Although the model and the field measurements suggest that anaerobic CH\textsubscript{4} oxidation may contribute to CH\textsubscript{4} consumption in the water column of Lake Pavin, aerobic oxidation remains the major sink of CH\textsubscript{4} in this lake.

1. Introduction

Methane can be considered both as an energy resource and as an atmospheric contaminant contributing to the greenhouse effect. Almost 2/3 of the current CH\textsubscript{4} emissions are anthropogenic and the present CH\textsubscript{4} concentration of 1.77 ppmv is more than twice its pre-industrial value. This global increase has contributed to an increase in radiative forcing (Solomon et al., 2007). Emission from wetlands is an important source of CH\textsubscript{4}, dominating natural sources of CH\textsubscript{4} in the atmosphere. In the past decade the overall annual rate of CH\textsubscript{4} growth has been reduced to nearly zero and has become highly variable. The decrease is attributed to a temporary reduction in anthropogenic emissions, while the increased variability is attributed to wetland emission (van Huissteden et al., 2008). For northern wetlands, it has been shown that at relatively high water tables, the CH\textsubscript{4} flux can change from net emission to net uptake (van Huissteden et al., 2005). Owing to the importance of this reversibility at the global scale, permanent or transient (seasonal) biogeochemical sink pathways need to be characterized.

In wetlands (watercourses, swamps, ponds and lakes) with anoxic, highly reductive conditions, the final stage of natural organic matter decomposition is CH\textsubscript{4} production (methanogenesis). Methanogens are strictly anaerobic microorganisms of the Archaea type utilizing very simple C compounds like acetate, CO\textsubscript{2} and methanol for their energy production (e.g., NO\textsubscript{3}, SO\textsubscript{4}\textsuperscript{2-}, Fe(III) and Mn(IV)) are available (Lovley and Phillips, 1987). Nevertheless, according to Crowe et al. (2010, and associated references), methanogenesis may account for a large part of organic matter recycling even in the presence of significant Fe(III) particle content, due to surface deactivation by Fe(hydro)oxides.

The CH\textsubscript{4} produced is partly consumed by methanotrophs, CH\textsubscript{4}-oxidising bacteria (Whiticar, 1993). Methane oxidation can occur aerobically or anaerobically in a wide variety of subsurface and surface environments. Anaerobic oxidation of methane (AOM) is a well-known mechanism in marine sediments (Elvert et al., 2000). For instance SO\textsubscript{4}-dependent methane oxidation (SDMO) (using SO\textsubscript{4}\textsuperscript{2-} as electron acceptor) has been reported in marine systems.

However, only a few lakes show the occurrence of anaerobic CH\textsubscript{4} oxidation (Joye et al., 1999; Eller et al., 2005; Ertefai et al., 2008). Recently, NO\textsubscript{3} and NO\textsubscript{2} have been found as suitable substrates for AOM in a freshwater canal sediment (Raghoebarsing et al., 2006). Moreover, Fe and Mn dependent anaerobic CH\textsubscript{4} oxidation (Fe/Mn-AOM) are presented as possible pathways of CH\textsubscript{4} consumption (Valentine, 2002). Recently, Crowe et al. (2010)
suggested that anaerobic CH$_4$ oxidation coupled to Fe or Mn reduction may occur in Lake Matano. Extreme conditions, such as high alkalinity or hypersalinity characterize most continental settings exhibiting anaerobic CH$_4$ oxidation, e.g., Big Soda Lake (Iversen et al., 1987), hypersaline Solar Lake (Cytryn et al., 2000) or continental mud volcanoes (Alain et al., 2006).

Meromictic lakes are usually small and widespread (Pourriot and Meybeck, 1995). They represent excellent field laboratories to follow biogeochemical reactions in permanently stratified ecosystems. Such a situation is found in Lake Pavin (Michard et al., 1994; Viollier et al., 1995) and makes this lake a unique microbial habitat allowing the study of biologically mediated redox processes. With an intense in situ production of Fe and Mn oxides (Viollier, 1995) and the presence of SO$_4^{2-}$ and NO$_3^-$ in the water column, chemical conditions potentially allow aerobic methanotrophy above the oxycline and anaerobic CH$_4$ oxidation beneath the oxycline. Based on the characterization of microbial communities (Lehours et al., 2005, 2007) and the utilization of a conservative tracer, Assayag et al. (2008) suggested that anaerobic CH$_4$ oxidation might explain the apparent CH$_4$ consumption in the mesolimnion of Lake Pavin. In order to numerically test the hypothesis of the CH$_4$ consumption pathways in Lake Pavin, field CH$_4$ oxidation rates were measured and a reactive transport model was developed. The model incorporates for the first time the CH$_4$ oxidation pathways coupled to the reduction of O$_2$, NO$_3^-$, SO$_4^{2-}$. Mn and Fe (hydr)oxides, with a set of classical primary and secondary redox reactions. In this study, the relative significance of the different CH$_4$ sink pathways in the water column of Lake Pavin are discussed.

2. Methods

2.1. Site description

Lake Pavin (elevation 1197 m above the sea level) is located in the French Massif Central at 45°29.74’N and 2°53.28’E in a volcanic area. It is circular in shape and has a diameter of 750 m and an area of 0.44 km$^2$. Its maximum depth is 92 m. It is a crater lake characterized by the presence of two stratified layers: the upper layer (the mixolimnion) which extends from the surface to 60 m depth and is affected by fall and spring turnover, and the deepest layer (monimolimnion) below approximately 70 m depth is permanent (the major physical and chemical parameters do not change seasonally) and anoxic. A transition zone, the mesolimnion (ca. 60–70 m depth), which separates the mixolimnion from the monimolimnion, is characterized by a strong increase in specific conductivity and an increase in temperature of about 1°C.

Within the mixolimnion three different layers can be identified based on seasonal depth variations of dissolved O$_2$, pH, temperature and conductivity: (1) The epilimnion corresponds to the surface mixed layer, with seasonal variations in temperature and thickness (0–20°C and 5–15 m), (2) the metalimnion (ca. 15–20 m depth) is characterized by a steep temperature gradient, (3) the hypolimnion with a stable temperature close to 4°C extends approximately from 20 to 60 m depth. Seasonal O$_2$ depletion down to zero occurs at the bottom of the hypolimnion within the depth range of approximately 58 and 61 m.

Fifteen tributaries, small or temporary, together with atmospheric precipitation contribute to surface water inputs (Table 1). Additional water supply comes from sublacustrine inputs (Table 1) to the mixolimnion (located at 54 ± 2 m depth, typical surface runoff water) and to the monimolimnion (located at 89 ± 2 m depth, typical mineral spring water) (Assayag et al., 2008). Biological diversity and activity have been described in Quiblier-Lloberas et al. (1996), Colombet et al. (2006) and Lemarchand et al. (2006).

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Lake Pavin biogeochemical model: fixed parameters.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
<td>Value</td>
</tr>
<tr>
<td>$\Delta_{H_2}$</td>
<td>5 mm$^2$</td>
</tr>
<tr>
<td>$\Delta_{O_2}$</td>
<td>5 mm$^2$</td>
</tr>
<tr>
<td>$\Delta_{OC}$</td>
<td>10 mm$^2$</td>
</tr>
<tr>
<td>$\Delta_{H_2}$ (March–April)</td>
<td>100 mm$^2$</td>
</tr>
<tr>
<td>$\rho_{mix}$</td>
<td>2820 kg m$^{-3}$</td>
</tr>
<tr>
<td>$\rho_{CH_4}$</td>
<td>1500 kg m$^{-3}$</td>
</tr>
<tr>
<td>Q, mixolimnion (34 m depth)</td>
<td>1728 m$^3$ day$^{-1}$</td>
</tr>
<tr>
<td>Q, monimolimnion (89 m depth)</td>
<td>138 m$^3$ day$^{-1}$</td>
</tr>
<tr>
<td>[Fe$^{II}$]$_{mix}$monimolimnion</td>
<td>0.56 mmol L$^{-1}$</td>
</tr>
<tr>
<td>[Mn$^{II}$]$_{mix}$monimolimnion</td>
<td>0.044 mmol L$^{-1}$</td>
</tr>
<tr>
<td>[SO$<em>4^{2-}$]$</em>{mix}$input</td>
<td>0.01 mmol L$^{-1}$</td>
</tr>
<tr>
<td>[NO$<em>3^-$]$</em>{mix}$input</td>
<td>0.03 mmol L$^{-1}$</td>
</tr>
<tr>
<td>[O$<em>2$]$</em>{mix}$input</td>
<td>0.33 mmol L$^{-1}$</td>
</tr>
<tr>
<td>$F_{-CH_4,40m}$</td>
<td>5.8 × 10$^{-3}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>$F_{-CH_4,92m}$</td>
<td>2.6 × 10$^{-3}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>$F_{Fe}^{ii}$</td>
<td>9.21 × 10$^{-4}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>$F_{Mn}^{ii}$</td>
<td>1.39 × 10$^{-6}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>$F_{NH_4}$</td>
<td>4.13 × 10$^{-4}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>$F_{H_2}$</td>
<td>6 × 10$^{-5}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>$F_{NO_2}$</td>
<td>1.6 × 10$^{-5}$ mol m$^{-2}$ day$^{-1}$</td>
</tr>
<tr>
<td>Q</td>
<td>1019–2630 m$^3$ day$^{-1}$</td>
</tr>
<tr>
<td>d</td>
<td>1–16 m$^3$</td>
</tr>
</tbody>
</table>

$\Delta_{H_2}$, $\Delta_{O_2}$, $\Delta_{OC}$ – Diameter of particulate Fe, particulate Mn and particulate organic C, respectively.

$\rho_{mix}$, $\rho_{CH_4}$ – Density of particulate Fe, Mn and organic C.

Q, mixolimnion, Q, monimolimnion – Flow rate of the mixolimnion and monimolimnion sublacustrine inflows (Assayag et al., 2008).

Q – Flow rate ranges of the small tributaries determined in field campaigns from June 2006 to June 2007.

$[SO_4^{2-}]_{mix}$, $[NO_3^-]_{mix}$, $[O_2]_{mix}$ – Average concentrations of SO$_4^{2-}$, NO$_3^-$ and dissolved O$_2$ of the tributaries and of the sublacustrine inflow in the mixolimnion.

$F_{-CH_4,40m}$ and $F_{-CH_4,92m}$ – Methane fluxes at 40 and 92 m depth calculated according to Fick’s law (Boudreau, 1997) with CH$_4$ concentration profiles in sediments collected at 40 and 92 m depth.

$F_{Fe}^{ii}$, $F_{Mn}^{ii}$, $F_{NH_4}$ – Fluxes of dissolved Fe, Mn and NH$_4^+$ determined according to Fick’s law with data from 1994 (Viollier, 1995).

$F_{Fe}^{ii}$, $F_{Mn}^{ii}$, $F_{NH_4}$ – Fluxes of particulate Fe and Mn from field data collected in 1994 (Viollier, 1995).

Based on Taffelet and Gaillard (2002).

Based on Pourriot and Meybeck (1995).

Assayag et al. (2008).

From this study.

From field data collected in September 1993 (Viollier, 1995).

From field data collected in 1994 (Viollier, 1995).

2.2. Data set: vertical concentration profiles from multiple campaigns

From June 2006 to June 2007, monthly water samples were taken along a vertical profile near the centre of the lake. Additionally, settling particles were collected from May 2006 to May 2007 with sediment traps at 23 m depth in order to determine particulate fluxes (Thiam et al., in preparation). Particles were collected approximately every month, except during winter 2006 (sediment traps were not sampled from November 2006 to mid March 2007). Sodium azide crystals were used as poison in order to prevent particle biodegradation. Immediately after sampling, settled particles were filtered on GF/F Whatmann membranes under a N$_2$ atmosphere.

Temperature, conductivity and dissolved O$_2$ concentration were measured with a Seabird Seacat Profiler SBE19. Depth profiles of NO$_3^-$ and SO$_4^{2-}$ concentrations were determined monthly. Methane concentration in the water column was determined in June 2006, September 2006, February 2007, April 2007, May 2007, June 2007 and July 2007 (see Section 2.2.1). Depth profiles of dissolved organic C were measured in October 2006, May and June 2007.
2.2.1. Methane concentrations in the water column and in sediment pore water

Water samples for CH₄ analysis were collected with an automatic laboratory-made 1 L syringe sampler along a vertical profile near the centre of the lake. Water from the oxic mixolimnion (from the surface to 55 m depth) was collected into serum bottles (100 mL) by filling them to overflowing, sealing and poisoning with 1 mL of 0.5 g L⁻¹ HgCl₂. A 30 mL N₂₂ headspace was created before analysis, as described in Abril and Iversen (2002). In the CH₄-rich monimolimnion (from 55 m to 90 m), a different sampling procedure was used in order to limit the loss of CH₄ due to depressurization: 30 mL of water from the sampling syringe were rapidly transferred with a needle through the butyl cap of a pre-weighed 100 mL serum bottle (pre flushed with N₂ gas). With this procedure, most of the depressurization occurred in the vial and the loss of CH₄ could be minimized. Methane concentrations were quantified using a gas chromatograph (GC) equipped with flame ionization detector (FID), according to Abril and Iversen (2002).

Site sediment cores from 40 and 92 m depth were sampled with a UWITEC corer (99 x 160 cm) in order to determine CH₄ concentration profiles in sediment pore waters for June 2007. Cores were laterally sub-sampled at 2 cm intervals with 2 mL syringe-based pistons, through pre-drilled holes in the tube corer (holes were initially closed with water-proof tape). Sediment sub-samples were then transferred into pre-weighed 100 mL serum bottles containing 10 mL of 10 N NaOH. The vials were then sealed rapidly with rubber stoppers and Al crimps. They were then weighed and shaken vigorously. The CH₄ concentration in the equilibrated gas phase was determined as for water samples. Methane concentration in pore waters was calculated using the water content (determined gravimetrically on duplicate cores). Methane fluxes from the sediment layer at 40 and 92 m were calculated according to Fick’s law (Boudreau, 1997; see Section 3.3 in this manuscript, Table 1).

2.2.2. In situ methane oxidation rates

In order to determine in situ anaerobic CH₄ oxidation rates, water samples were collected from 60, 61 and 62 m depths, transferred to serum bottles and incubated at their respective depths using nylon bags attached to a float-wire cable. Additionally, some vials from each depth were poisoned with HgCl₂ (1 mL of 0.5 g L⁻¹ HgCl₂), in order to inhibit the activity of CH₄ oxidizers, representing a reference for potential abiotic evolution. Sample bottles were removed from the water column in May 2007. Rates were calculated from the difference in CH₄ concentrations between October 2006 and May 2007.

Aerobic CH₄ oxidation rates were determined at variable CH₄ concentrations. Three litres of water were collected at 50 m depth and about 800 mL were transferred to three 1 L glass vials containing 200 mL of air headspace. A known amount of pure CH₄ was then introduced in the headspace and the vials were vigorously shaken in order to equilibrate the CH₄ in the water and the gas mixture. Three different CH₄ concentrations were tested: 60 x 10⁻⁹, 171 x 10⁻⁹ and 352 x 10⁻⁹ mol L⁻¹, covering the range of water CH₄ concentrations in the upper layers of the mixolimnion (from the surface to approximately 55 m). Water samples were then siphoned into 100 mL serum vials that were further sealed. In the assays, O₂ was not limiting. Eight bottles for each CH₄ concentration were incubated at in situ temperature. At 0, 22, 36 and 51 h, duplicate bottles were poisoned with HgCl₂, and further analyzed for CH₄ initial concentration as described earlier. Rates of aerobic CH₄ oxidation for each CH₄ concentration were calculated as the slope of the decrease in CH₄ concentration with time. The first order constant of the aerobic CH₄ oxidation kinetics was subsequently determined and used in the reactive transport model (see below).

2.3. Model description

2.3.1. Overview

A reactive-transport model that accounts for spatial and temporal distribution of chemical species in the lake water column was developed from AQUASIM software (Reichert, 1998).

In the model, dissolved and particulate species are transported through the water column by vertical mixing. Particulate substances are also transported by sedimentation. Moreover, dissolved species are brought to the lake by inflows from small tributaries and by sublacustrine inputs. Dissolved and particulate species are allowed to react in multiple biogeochemical pathways specified through reaction rate equations.

2.3.2. Modelled species (state variables)

The model considers the following state variables: CH₄, dissolved and particulate Fe and Mn, dissolved O₂, NO₃, SO₄²⁻, NH₄⁺, total dissolved sulfide, dissolved and particulate organic C (DOC and POC, respectively), total orthophosphates and total dissolved CO₂ (DIC). The elemental composition of organic ions is similar to the one reported by Sigg (1985) for lake Constance: (CH₂O)₉₁₃[NH₃]₁₅[H₃PO₄].

2.3.3. Governing differential equations

Biogeochemical and physical processes, expressed by a set of partial differential transport-reaction equations (Reichert, 1998), are implemented in the AQUASIM code. The following equations are solved for each dissolved and particulate state variable, respectively.

\[
\frac{\partial C}{\partial t} = \frac{\partial}{\partial z} \left( AK \frac{\partial C}{\partial z} \right) - \frac{\partial}{\partial z} \left( QC \right) + r_C + \frac{q}{A} C_{in} \tag{1}
\]

\[
\frac{\partial X}{\partial t} = \frac{\partial}{\partial z} \left( AK \frac{\partial X}{\partial z} \right) - \frac{\partial}{\partial z} \left( QX \right) + r_X + \frac{\partial}{\partial z} \left( V_{sed} X \right) \tag{2}
\]

where C is the concentration of a dissolved compound (M L⁻³), X is the concentration of a particulate compound (M L⁻³), t is the time (T), z is the vertical coordinate pointing downwards (z = 0 at the lake surface) (L), A is the cross-sectional area of the lake (L²), K is the vertical mixing coefficient (L² T⁻¹), r are the transformation rates (M L⁻³ T⁻¹), Q is the vertical discharge induced by water inflows in the lake depth (L T⁻¹), Cₘₙ is the inflow concentration of a dissolved compound (M L⁻³), Vₘₙ is the sedimentation velocity (L T⁻¹), q is the discharge of water per unit depth into the lake (L T⁻¹).

In both equations, the first term describes mixing due to eddy diffusion, the second term refers to advection in the water column resulting from inflows, and the third term describes the net effect of all transformations processes. In Eq. (1), the fourth term is related to inflows, whereas in Eq. (2), it describes sedimentation of particulate species through the water column. Other boundary conditions are the benthic fluxes of iron, manganese and ammonium from sediment pore waters, calculated according to Fick’s law (Boudreau, 1997) and field data from September 1993 (Viollier, 1995). The set of partial differential equations is solved numerically with a vertical resolution of 1 m (Reichert, 1998).
2.3.4. Physical processes

2.3.4.1. Vertical mixing. Monthly vertical eddy diffusion coefficient ($K_z$) profiles are calculated based on temperature and conductivity profiles. Water column density and Brunt-Väisälä Frequency ($N^2$) are calculated according to expressions reported by Aeschbag-Hertig et al. (2002). The vertical resolution is 1 m. The following expression is used to derive $K_z$ values:

$$K_z = \alpha (N^2)^{-q}$$

where $K_z$ is the vertical eddy diffusion coefficient (M$^2$ T$^{-1}$) and $N^2$ is the Brunt-Väisälä (T$^{-2}$) frequency given by:

$$N^2 = \frac{\gamma \partial \rho}{\rho \partial z}$$

The parameter $q$ is set to 0.5 as discussed in Aeschbag-Hertig et al. (2002) for Lake Pavin. Eddy diffusion coefficient values in Lake Pavin spread over 4 orders of magnitude. The smallest values are calculated for the mesolimnion where $K_z$ decreases to nearly $10^{-8}$ m$^2$ s$^{-1}$.

2.3.4.2. Advection. Advection fluxes are directly related to the sublacustrine inflows. In the mixolimnion, NO$_3$, SO$_4^{2-}$, and O$_2$ are constantly brought to the water column. In the monimolimnion, the mineral spring located at 89 ± 2 m depth adds dissolved Fe and Mn to the lake (Viollier et al., 1997) (Table 1). Advection appears to be fairly weak with average rates from few centimeters to meters per year when normalized to the lake cross section (Michard et al., 1994). In the epilimnion, advection is also impacted by the small tributaries (Table 1). The equal-density level is used to determine the diving depth of those lateral inputs.

2.3.4.3. Sedimentation. Sedimentation rate of particulate Fe, Mn and organic C are calculated according to Stokes’s law (Talliefer and Gaillard, 2002). Monthly sedimentation rate profiles for these species are calculated based on water column density, water viscosity, size and density of the particles. Average density and diameter of particulate Fe, Mn and organic C are presented in Table 1. The increase of the average diameter of the organic C particles from middle March to middle April is taken into account. It corresponds to Diatom spring bloom (main species: *Aulacoseira italica*, *Asterionella formosa*) and aggregation-sedimentation processes leading to an increase in sedimentation velocity (Carrias, 1996). The calculated sedimentation velocities of particulate Fe and Mn ranged from 0.55 m day$^{-1}$ in lower water layers (for all months) to 0.55–0.9 m day$^{-1}$ in the epilimnion (values for April 2007 and July 2006, respectively).

Sedimentation velocities of POC of 0.2–40 m day$^{-1}$ are described in the literature (Pourriot and Meybeck, 1995; Omlin et al., 2001). The calculated POC sedimentation rates in this work ranged from 1.5 m day$^{-1}$ in the lower water layers to 1.7–2.3 m day$^{-1}$ in the upper water layers (values for April 2007 and June 2006, respectively). From March 2007 to April 2007, particulate organic C sedimentation rates ranged from 6 m day$^{-1}$ for layers below the hypolimnion to around 6–6.4 m day$^{-1}$ in the epi- and metalimnion.

Additionally, particulate Fe and Mn fluxes from the surface of the lake are also included in the model. Data were measured elsewhere ($6 \times 10^{-5}$ and $1.6 \times 10^{-3}$ mol m$^{-2}$ day$^{-1}$ for particulate Fe and particulate Mn, respectively) from the 1994 data set published in Viollier et al., 1995 (Table 1).

2.3.4.4. Gas exchange at the lake surface. Dissolved O$_2$, CO$_2$ and CH$_4$ exchange rates are considered as boundary conditions at the lake surface. The dissolved O$_2$ flux, given by Eq. (5), is proportional to the difference between O$_2$ concentration ($O_{2,z-o}$) at the lake surface and the saturation concentration ($O_{2,solubility}$) corrected to the elevation above sea level:

$$F_{O_2} = k \times (O_{2,solubility} - O_{2,z-o})$$

where $F_{O_2}$ is the O$_2$ flux (mol m$^{-2}$ day$^{-1}$) and $k$ is the gas exchange velocity, which is proportional to the square of wind velocity (m day$^{-1}$) (Liss and Merlivat, 1986). $k$ equals 1 m day$^{-1}$. $O_{2,z-o}$ and $O_{2,solubility}$ are given in mol m$^{-3}$.

The partial pressure of O$_2$ in air is assumed constant and equal to 0.21 times the atmospheric pressure (about 880 mbar) at the elevation of the lake.

The dependence of the saturation concentration of O$_2$ (mol L$^{-1}$) on temperature is given by the following expression:

$$O_2 = 10^{-0.47238 + 0.0061403 \log(T - 273)} \times 0.2095 \exp(-0.000119H)$$

where $T$ is the water temperature in °C at the lake surface and $H$ describes the elevation of the lake above sea level (1200 m).

The CO$_2$ flux across the water–air interface is also proportional to the difference of the current CO$_2$ ($CO_{2,z-o}$) at the lake surface and the saturation (CO$_{2,solubility}$) value.

$$F_{CO_2} = k \times (CO_{2,solubility} - CO_{2,z-o})$$

where $F_{CO_2}$ is the CO$_2$ flux (mol m$^{-2}$ day$^{-1}$), $k$ (1 m day$^{-1}$) is the gas exchange velocity (the same as Eq. (5)). $CO_{2,z-o}$ and $CO_{2,solubility}$ are given in mol m$^{-3}$. CO$_2$ is calculated from the DIC (dissolved inorganic C), the water pH and $K_1$ and $K_2$ (dissociation constants).

The partial pressure of CO$_2$ in air is assumed constant and equal to $3.7 \times 10^{-4}$ the atmospheric pressure at the elevation of the lake. The saturation concentration of CO$_2$ is given by the following equation (Robie et al., 1978):

$$CO_{2,solubility} = 0.001 \times (25.05 - 0.8249T + 0.0011327T^2)$$

where CO$_{2,solubility}$ is given in mol m$^{-3}$ and $T$ is the water temperature in °C at the lake surface.

The dissolved CH$_4$ flux (mol m$^{-2}$ day$^{-1}$) is given by the following expression:

$$F_{CH_4} = k \times (CH_{4,solubility} - CH_{4,z-o})$$

where

$$CH_{4,solubility} = K_H P_{CH_4}$$

with $K_H$ is the Henry’s law constant (mol L$^{-1}$ atm$^{-1}$; Sanders, 1999)

$$K_H = 1.4 \times 10^{-3} \exp \left[ \frac{\text{-}7100 \times \left( \frac{1}{T + 273} - \frac{1}{298.15} \right)}{298.15} \right]$$

and $P_{CH_4}$ is the CH$_4$ partial pressure in the air (approximately $2 \times 10^{-6}$ atm).

2.3.5. Biogeochemical reactions

2.3.5.1. Redox reactions. The set of reactions used in the model is adapted from those proposed by Hunter et al. (1998), Van Cappellen and Wang (1996), Omlin et al. (2001) and Reichert et al. (2001) for surface and subsurface environments. Table 2 gives an overview of the biogeochemical processes used in the model. The model includes the organic C export reaction (Reaction (1)), primary redox reactions, i.e. organic matter mineralisation of dissolved and particulate organic C (Reactions (2)–(7)) and the secondary redox reactions (Reactions (8)–(19)). Primary reactions include aerobic respiration (Reaction (2)), denitrification (Reaction (3)), Mn oxide reduction (Reaction (4)), Fe (hydr)oxide reduction (Reaction (5)), SO$_4^{2-}$ reduction (Reaction (6)) and methanogenesis (Reaction (7)). Oxidation of organic matter produces reduced species such as Mn$^{2+}$, Fe$^{2+}$ and CH$_4$ which may participate in secondary redox reactions. The model considers the following secondary reactions:
nitrification (Reaction (18)), Fe oxidation (Reaction (13)), Mn oxidation (Reaction (16)), Fe oxidation through reaction with Mn oxides (Reaction (14)), Fe reduction coupled to denitrification (ferrous denitrification, Reaction (15)), sulfide oxidation (Reaction (19)), nitrification coupled to Mn oxides reduction (17). The following CH₄ consumption pathways are integrated in the model: aerobic CH₄ oxidation (Reaction (8)) and anaerobic CH₄ oxidation associated with denitrification (Reaction (9)), Mn (Reaction (10)), Fe (Reaction (11)) and SO₄²⁻ reduction (Reaction (12)).

All the process rates are given in Table 3. The degradation of dissolved and particulate organic C is driven by microbially mediated processes. One appropriate expression for the dependence of organic C degradation on the electron acceptor concentration, such as dissolved O₂ or NO₃⁻, is the Monod rate law (Van Cappellen et al., 1993; Boudreau, 1997). The presence of some oxidants may inhibit other metabolic pathways. Inhibition by oxidants is represented by an additional term in rate Eqs. (13)-(27) (Boudreau, 1997; Regnier et al., 2006). Once the concentration of the inhibitory species increases, the value of the inhibition term decreases and the effective rate decreases as well. The use of the limiting and inhibition functions in the model provides a direct coupling between the transformation processes and multiple species. The rate of methanogenesis (Eqs. (17) and (23)) is modelled as being inhibited by all oxidants. The same principle of inhibition terms is applied to the CH₄ oxidation kinetics. Calculation of the standard Gibbs energy of Reactions (8)-(12) showed that the most energetically favourable pathway is the CH₄ aerobic oxidation, followed by denitrification, Mn, Fe and SO₄²⁻ reductions. Secondary redox reactions (Reactions (11)-(14), Reactions (16) and (19), Table 2) are represented by bimolecular rate law (Table 3), with apparent rate coefficients (Hunter et al., 1998; Smith and Jaffé, 1998).

In contrast to the primary and secondary redox reactions described in Table 2 for which rates are shown in Table 3, the organic C export rate (Reaction (1)) is derived from total organic C measurements in sediment traps collected at 23 m depth from May 2006 to May 2007 (Fig. 1). The organic C export rate generates particulate and dissolved organic C. The fraction of dissolved organic C is arbitrarily set at 10% of the particulate organic C produced in the epilimnion (Reichert et al., 2001).

2.3.5.2. Acid–base reactions. In contrast to redox reactions, acid-base reactions reach equilibrium almost instantaneously. Although the AQUASIM code can solve algebraic equations, classic calculation of pH in a dynamic system frequently leads to numerical problems. In order to calculate water column pH, the following equations were implemented:

\[
R_b = R_{b0} + [\text{NH}_4^+]^+ - [\text{NH}_4^+] - 2[\text{Fe}^{2+}]^+ - 2[\text{Fe}^{2+}]_{\text{ox}} + 2[\text{Mn}^{2+}]^+ \]

(38)

where the alkaline reserve, \(R_b\), stands for the sum of nonreactive species (Na⁺, K⁺, Ca²⁺, Mg²⁺, Cl⁻) as follows:

\[
R_b = [\text{Na}^+]^+ + [\text{K}^+]^+ + 2[\text{Ca}^{2+}]^+ + 2[\text{Mg}^{2+}]^+ - [\text{Cl}^-]^{-} \]

(39)

and the sum of species which are consumed or produced by the redox reactions: inactive acids or bases (NO₃⁻, SO₄²⁻) or species which are assumed as inactive in the conditions of the lake (NH₄⁺, Mn²⁺, Fe⁺³) (Michard, 1989). In fact, the latter species are only found in the reduced and relatively acid layers where the pH (<7.5) is significantly lower than the pKa of these acids. \(R_b\) is the algebraic sum of the charges of produced and/or un consumed charged species. The \(R_b\) only changes with the difference between river inflows and outflows. The subscript “0” indicates the concentration of each chemical species at the initial time.

With \(R_b\) and DIC values, proton activity is calculated by Eq. (40):

\[
R_b / \text{DIC} = (1 + 2K_{a2}/H^+)/(1 + H^+/K_{a1} + K_{a2}/H^+) \]

(40)

where \(K_{a1}\) and \(K_{a2}\) are the equilibrium constants of the chemical equilibria between CO₂ and HCO₃⁻ and between HCO₃⁻ and CO₃²⁻, respectively. It should be stressed that Eq. (40) is valid for a water column pH lower than 9.5, which is consistent with the maximum pH values reported in Lake Pavin (Michard et al., 1994; Assayag et al., 2008).

2.3.6. Initial conditions

Initial conditions for concentrations of dissolved species in the water column are those observed on June 17, 2006, except for dissolved and particulate Fe and Mn, POC, DIC and pH. Particulate Fe, Mn and DIC concentration profiles were measured in September 1993 (Viollier, 1995). Dissolved Fe, Mn and pH were determined in 1993 (Viollier, 1995). The initial POC profile was determined in June 1973 (Devaux et al., 1983) but it was not case-sensitive.

2.3.7. Modelling approach

Model calculations were performed starting from the 17th of June 2006 and simulations were carried out over 1 year. In model calculations half-saturation coefficients in Monod-type expressions and the maximum rates of the processes described in Table 3 are based on values reported in the literature (e.g. Hunter et al., 1998; Smith and Jaffé, 1998; Lidstrom and Somers, 1984; Smith et al., 1991; Omlin et al., 2001). The kinetic parameters of the biogeochemical processes (see “a” – fitted parameters in Table 4)
were iteratively changed by a trial-and-error approach until simulations led to visual fit agreement with measurements of monthly depth profiles of CH$_4$, dissolved O$_2$, NO$_3^-$, SO$_4^{2-}$, and whenever available, dissolved organic C, dissolved Fe, dissolved Mn and NH$_4^+$. Early diagenesis of organic matter was not implemented in the model and the benthic contribution was taken into account through benthic boundary conditions. For instance, benthic flux of CH$_4$ had to be increased by a factor of two compared with the field estimation (Tables 1 and 4). Owing to the large uncertainty of the field derived value (possible CH$_4$ loss, centimetre-scale gradient resolution only), this adjustment remains acceptable. Following model calibration, depth concentration profiles of particulate organic C predicted by the model were compared with data obtained from field campaigns in 1992 (Carriás, 1996; Carriás et al., 1998).

### 2.3.8. Sensitivity analysis

A sensitivity analysis was performed in order to determine the model sensitivity to imperfect knowledge of (1) some kinetic parameters related to the CH$_4$ pathways ($K_{CH4,Fe}$, $K_{CH4,Mn}$, $K_{CH4,DOC}$, $K_{CH4,NO3}$, $K_{CH4,NO2}$ and NO$_{lim}$) and (2) vertical mixing (eddy diffusion coefficient $K_z$). The relative uncertainties of the kinetic parameters were assumed to be 50% and the eddy diffusion coefficients

<table>
<thead>
<tr>
<th>Table 3</th>
<th>Lake Pavin biogeochemical model: kinetic equations.</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_{degCH4}$ = $K_{CH4,CO2}$ × CH$_4$ × O$_2$</td>
<td>12</td>
</tr>
<tr>
<td>$r_{degCH4,NO3}$ = $K_{CH4,NO3}$ × CH$_4$ × NO$_3$</td>
<td>13</td>
</tr>
<tr>
<td>$r_{degCH4,Mn}$ = $K_{CH4,Mn}$ × Mn$_p$ × CH$_4$</td>
<td>14</td>
</tr>
<tr>
<td>$r_{degCH4,SO4}$ = $K_{CH4,SO4}$ × SO$_4$ × CH$_4$</td>
<td>15</td>
</tr>
<tr>
<td>$r_{DOC,CH4}$ = $K_{DOC,CH4}$ × DOC × CH$_4$</td>
<td>16</td>
</tr>
<tr>
<td>$r_{DOC,SO4}$ = $K_{DOC,SO4}$ × DOC × SO$_4$</td>
<td>17</td>
</tr>
<tr>
<td>$r_{DOC,Fe}$ = $K_{DOC,Fe}$ × DOC × Fe$_3$</td>
<td>18</td>
</tr>
<tr>
<td>$r_{DOC,Mn}$ = $K_{DOC,Mn}$ × Mn$_p$ × DOC</td>
<td>19</td>
</tr>
<tr>
<td>$r_{DOC,NO3}$ = $K_{DOC,NO3}$ × NO$_3$ × DOC</td>
<td>20</td>
</tr>
<tr>
<td>$r_{DOC,Fe}$ = $K_{DOC,Fe}$ × Fe$_3$ × O$_2$</td>
<td>21</td>
</tr>
<tr>
<td>$K_{Fe,2-0}$ = 2×10$^{-6}$</td>
<td>22</td>
</tr>
<tr>
<td>$r_{Fe^{2+},Mn}$ = $K_{Fe^{2+},Mn}$ × Fe$^{2+}$ × Mn$_p$</td>
<td>23</td>
</tr>
<tr>
<td>$r_{Fe^{2+},O_2}$ = $K_{Fe^{2+},O_2}$ × Fe$^{2+}$ × O$_2$</td>
<td>24</td>
</tr>
<tr>
<td>$K_{Fe,2-0}$ = 2×10$^{-6}$</td>
<td>25</td>
</tr>
<tr>
<td>$r_{NH4^+,Mn}$ = $K_{NH4^+,Mn}$ × NH$_4^+$ × Mn$_p$</td>
<td>26</td>
</tr>
<tr>
<td>$r_{NH4^+,O_2}$ = $K_{NH4^+,O2}$ × NH$_4^+$ × O$_2$</td>
<td>27</td>
</tr>
<tr>
<td>$r_{CH4,Fo}$ = $K_{CH4,Fo}$ × CH$_4$ × O$_2$</td>
<td>28</td>
</tr>
</tbody>
</table>

Where $K_r$ – kinetic parameter, O$_2$ – oxygen concentration (M L$^{-3}$), CH$_4$ – methane concentration (M L$^{-3}$), Mn$_p$ – particulate manganese concentration (M L$^{-3}$), Fe$_3$ – particulate iron concentration (M L$^{-3}$), SO$_4$ – sulphate concentration (M L$^{-3}$), DOC – dissolved organic carbon concentration (M L$^{-3}$), POC – particulate organic carbon concentration (M L$^{-3}$), H$^+$ – hydrogen ion concentration (M L$^{-3}$), NO$_3^-$ – total dissolved sulfide concentration (M L$^{-3}$), Fe$^{2+}$ – dissolved iron concentration (M L$^{-3}$), Mn$^{2+}$ – dissolved manganese concentration (M L$^{-3}$), NH$_4^+$ – ammonium concentration (M L$^{-3}$), NO$_{lim}$ – maximum nitrate concentration in the water column (M L$^{-3}$), O$_{lim,CH4}$ – oxygen limiting concentration for aerobic methane oxidation (M L$^{-3}$), O$_{lim}$ – half-saturation coefficient for nitrification (M L$^{-3}$), NO$_{lim}$ – half-saturation coefficient for oxygen limiting concentration for organic matter degradation (M L$^{-3}$), S$^{2-}$ – total dissolved sulfide concentration (M L$^{-3}$), O$_2$ – oxygen concentration (M L$^{-3}$), Mn$^{2+}$ – oxygen half-saturation coefficient for nitrification (M L$^{-3}$).
were doubled. In the first step, these parameters were analyzed separately. In the second step, the impact of uncertainties of all the kinetic parameters of the CH₄ degradation pathways was tested (half-saturation coefficients, maximum rates and inhibition factors, see Table 3).

3. Results

3.1. Limnology

From a geochemical point of view, the upper layer of the mixolimnion is oxygenated with a pH that can vary from 8 to 9 above the thermocline (Michard et al., 1994). Temperature at the lake surface varied from 3.4 °C in February 2007 (data not shown) to 22 °C in July 2006 (Fig. 2). During the winter 2006–2007, the mixolimnion was vertically thoroughly mixed from January to February 2007. Lower layers in the mixolimnion (from 20 m to 55 m) have a constant temperature of 4 °C all year long. From 60 m depth, an increase in temperature is observed due to the geothermal flux and turbulent heat exchange restriction between the monimolimnion and the mixolimnion (temperature = 5.06 °C at the bottom of the lake). This limitation is illustrated in Fig. 3 which shows conductivity profiles in Lake Pavin from June 2006 to June 2007. As expected, a permanent zone of strong chemical gradient is observed from approximately 60 to 70 m depth. Fairly weak eddy diffusion coefficients in this layer are essentially related to the corresponding strong density gradient.

3.2. Methane in the water column

Fig. 4a presents CH₄ concentration profiles from June 2006 to June 2007. Methane concentrations increase sharply at approximately 55 m depth to reach $4 \times 10^{-3}$ mol L⁻¹ at 92 m depth. Differences in CH₄ concentrations for the deepest layers are observed in June 2007 but globally from 30 years of observations, the monimolimnion is considered to have reached interannual steady state (Vioillier et al., 1997; Michard et al., 2003). However, significant increase of CH₄ is also observed in the epilimnion (Fig. 4b). Fig. 5 a and b show the overlapping concentration profiles of CH₄, O₂, NO₃⁻ and SO₄²⁻ for June 2006 at the boundary between the monimolimnion and the mesolimnion. Also overlapping concentration profiles of particulate Fe and Mn measured in September 1993 are given in Fig. 6 for the same layers. These results underline the possibility that CH₄ can react aerobically or anaerobically with multiple substrates in Lake Pavin.

3.3. Methane in sediment

The CH₄ concentration profile in the sediment collected at 40 m depth is presented in Fig. 7. From this profile and the one at 92 m depth (data not shown), CH₄ flux from the sediment was calculated

---

**Table 4**

Lake Pavin biogeochemical model: kinetic constants and adjusted parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K_{CH4,TV}$</td>
<td>0.005 mol⁻¹ m⁻³ day⁻¹</td>
</tr>
<tr>
<td>$Q_{2lim}$</td>
<td>0.02 mol m⁻³</td>
</tr>
<tr>
<td>$Q_{2lim,CH4}$</td>
<td>0.02 mol m⁻³</td>
</tr>
<tr>
<td>NO₃lim</td>
<td>0.005 mol m⁻³</td>
</tr>
<tr>
<td>NO₃max</td>
<td>0.0032 mol m⁻³</td>
</tr>
<tr>
<td>NO₃min</td>
<td>0.01 mol m⁻³</td>
</tr>
<tr>
<td>$K_{CH4,Mn}$</td>
<td>0.05 m⁻³ mol⁻¹ day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,SO4}$</td>
<td>0.0274 m⁻³ mol⁻¹ day⁻¹</td>
</tr>
<tr>
<td>$F_{CH4}$</td>
<td>0.0032 mol m⁻³</td>
</tr>
<tr>
<td>SO₃lim</td>
<td>0.03 mol m⁻³</td>
</tr>
<tr>
<td>$K_{CH4,SO4}$</td>
<td>0.03 mol m⁻³ day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,NO3}$</td>
<td>0.0006 mol m⁻³</td>
</tr>
<tr>
<td>$K_{CH4,C2}$</td>
<td>0.14 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,DOC}$</td>
<td>0.00014 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,POR}$</td>
<td>0.00047 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,POC}$</td>
<td>0.00047 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,DOC}$</td>
<td>0.00014 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,POC}$</td>
<td>0.000027 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,DOC}$</td>
<td>0.000027 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,POC}$</td>
<td>0.01 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH3,DOC}$</td>
<td>0.01 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH2,DOC}$</td>
<td>0.01 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH2,POC}$</td>
<td>0.04 day⁻¹</td>
</tr>
<tr>
<td>$K_{CH2,NO3}$</td>
<td>0.0274 m³ mol⁻¹ d⁻¹</td>
</tr>
<tr>
<td>$K_{CH2,NO3}$</td>
<td>0.01 m³ mol⁻¹ day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,NO3}$</td>
<td>0.001 m³ day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4,C2}$</td>
<td>0.001 m³ mol⁻¹ day⁻¹</td>
</tr>
<tr>
<td>$K_{CH4}$</td>
<td>0.0064 mol m⁻³</td>
</tr>
<tr>
<td>$K_{CH4}$</td>
<td>0.025 mol m⁻³</td>
</tr>
<tr>
<td>$K_{CH4}$</td>
<td>0.438 mol m⁻³ mol⁻¹ day⁻¹</td>
</tr>
<tr>
<td>$F_{CH4,CH4}$</td>
<td>$5.2 \times 10^{-1}$ mol m⁻³ day⁻¹</td>
</tr>
</tbody>
</table>


a Fitted parameter.

b In the model, DOC is assumed highly biodegradable. Therefore, kinetic parameters of DOC degradation were initially assumed to be tenfold higher than those of POC biodegradation. Some of these parameters were then modified in order to achieve a good fit of the data and the model predictions.
by applying Fick’s first law of diffusion. The measured dissolved CH$_4$ concentration in the water at 40 m depth was about 0.08 × 10$^{-6}$ mol L$^{-1}$. Using a porosity value of 0.98 (Viollier, 1995), one can calculate the sediment diffusion coefficient of CH$_4$ (8.2 × 10$^{-5}$ m$^2$ day$^{-1}$) at 4 °C (Boudreau, 1997). Resulting benthic fluxes from the sediments at 40 m and 92 m depths were 5.8 × 10$^{-4}$ and 2.6 × 10$^{-3}$ mol m$^{-2}$ day$^{-1}$ (Table 1), respectively.

3.4. Methane oxidation in the water column

Measured rates of aerobic CH$_4$ oxidation varied between 6.2 × 10$^{-9}$ and 4.6 × 10$^{-8}$ mol L$^{-1}$ day$^{-1}$ for CH$_4$ concentrations ranging from 0.06 × 10$^{-6}$ to 0.35 × 10$^{-6}$ mol L$^{-1}$. The rate of CH$_4$ oxidation displayed first-order kinetics with respect to CH$_4$ concentration ($r^2 = 0.92$; $r_{CH4-O2}$ (mmol L$^{-1}$ day$^{-1}$) = 0.14 × [CH$_4$]) with an excess of O$_2$ (no limiting effect).

Since O$_2$ is a key factor in the aerobic CH$_4$ oxidation, its influence on the kinetics of this reaction is taken into account by considering an additional term O$_2$/O$_2$-solubility (Eq. (12), Table 3). This modified kinetics was then implemented in the model (Tables 3 and 4).

Moreover, at 60 and 62 m depth, a net CH$_4$ loss of 0.4 × 10$^{-6}$ mol L$^{-1}$ day$^{-1}$ was measured for 285 × 10$^{-6}$ and 785 × 10$^{-6}$ mol L$^{-1}$ initial CH$_4$ concentrations, respectively. These results suggest that anaerobic CH$_4$ oxidation may occur in the water column of Lake Pavin.

3.5. Model results

3.5.1. Species concentration in the water column

Measured and simulated concentration profiles of CH$_4$, NO$_3^-$, SO$_4^{2-}$ and O$_2$ in June 2007 are compared in Fig. 8a. General trends are qualitatively reproduced by the simulation. However, higher concentrations of NO$_3^-$ and SO$_4^{2-}$ were encountered between 40 and 60 m depth compared with the values expected from the model. The effect of the sublacustrine input within this depth range, by the addition of NO$_3^-$ and SO$_4^{2-}$ into the water column, may explain these discrepancies.

In Fig. 8b, POC concentration profiles in the mixolimnion calculated for August, October, November 2006 and April 2007 were compared to data measured in 1992 (Carrias, 1996; Carrias et al., 1998). It can be seen that POC model predictions are of the same order of magnitude as the data measured at 1, 5, 10, 15 and 40 m depths in the field campaigns of 1992.
3.5.2. Methane oxidation in the water column

Fig. 9 shows calculated rates of CH$_4$ oxidation in February and in June 2007. These two examples were chosen in order to evaluate the effect of winter mixing in CH$_4$ consumption and production pathways. An overlap between aerobic and anaerobic pathways is observed. Additionally, a seasonal difference between aerobic and anaerobic rates can be detected. In June 2007, aerobic CH$_4$ oxidation occurs in a narrow zone at the boundary of oxic–anoxic layers. In contrast, in February, aerobic CH$_4$ oxidation occurs in the upper layers of the mixolimnion. Winter mixing led to higher flux of CH$_4$ towards the upper layers of the mixolimnion and consequently to higher CH$_4$ concentrations (Fig. 10). This allows aerobic CH$_4$ oxidation to occur at higher rates compared to those of the stratified period.

Vertical distribution of the anaerobic CH$_4$ oxidation pathways is shown in Fig. 11. Rates of Mn dependent oxidation of CH$_4$ are not presented because they are extremely low compared with those of the other electron acceptors. This is mainly due to the low concentration of Mn oxides in the water column. The highest rate of AOM observed at a depth of approximately 60 m corresponds to NO$_3$ reduction. This metabolism explains the overlap between aerobic and anaerobic CH$_4$ oxidation pathways shown in Fig. 9. Anaerobic CH$_4$ oxidation by Fe and SO$_4^{2-}$ also contribute to anaerobic CH$_4$ consumption in the water column.
3.5.3. Sources and sinks of methane in Lake Pavin

In order to have a broader picture of methane sinks and sources in Lake Pavin, depth-integrated rates of CH$_4$ production and consumption for the entire water column in February and in June 2007 are presented in Table 5. Accordingly, a net consumption of CH$_4$ in the water column is reported. Aerobic CH$_4$ oxidation is the most significant CH$_4$ consumption pathway, contributing to 74% and 67% of the total CH$_4$ degradation in the water column in February and in June 2007, respectively, followed by denitrification (21% and 27% in February and in June, respectively) and Fe reduction (4% and 5% in February and June, respectively). Model calculations estimated a net flux of CH$_4$ to the atmosphere in February ($0.2 \times 10^{-3} \text{ mol m}^{-2} \text{ day}^{-1}$) and a negligible flux to the lake in June ($3 \times 10^{-6} \text{ mol m}^{-2} \text{ day}^{-1}$). Methane production in the water column is also proposed by the calculations (Table 5).

3.5.4. Sensitivity analysis

Simulations showed that variability in the tested kinetic parameters did not significantly affect the modelled species profiles. Moreover, changes in the CH$_4$ concentration profiles were observed when the eddy diffusion coefficients were doubled. Slight changes were detected in the modelled profiles of the other dissolved parameters and particulate species. The aerobic and anaerobic CH$_4$ oxidation rates were also sensitive to vertical mixing variability.

A sensitivity analysis was performed to evaluate the effect of the combination of all kinetic parameters of the CH$_4$ oxidation pathways on the rates of CH$_4$ oxidation. The possibility of compensation of an effect on the results caused by a change of one parameter in the set by an appropriate change of the other parameter may occur.
Table 5

Depth integrated sources (positive values) and sinks (negative values) of CH₄ in February and June 2007, compared with CH₄ stock in the water column.

<table>
<thead>
<tr>
<th>Process</th>
<th>February 2007</th>
<th>June 2007</th>
</tr>
</thead>
<tbody>
<tr>
<td>Aerobic CH₄ oxidation</td>
<td>-1.7 x 10⁻²</td>
<td>-6 x 10⁻²</td>
</tr>
<tr>
<td>Anaerobic CH₄ oxidation</td>
<td>-6 x 10⁻²</td>
<td>0.02 x 10⁻²</td>
</tr>
<tr>
<td>CH₄ production in the water column</td>
<td>1 x 10⁰</td>
<td>1 x 10⁰</td>
</tr>
<tr>
<td>CH₄ flux from the sediment</td>
<td>8 x 10⁻²</td>
<td>8 x 10⁻²</td>
</tr>
<tr>
<td>CH₄ water-air exchange</td>
<td>-0.7 x 10⁻²</td>
<td>-0.02 x 10⁻²</td>
</tr>
<tr>
<td>CH₄ stock (mol)</td>
<td>10 x 10⁰</td>
<td>10 x 10⁰</td>
</tr>
</tbody>
</table>

Methanogenesis and oxidation rates are normalized to volume and depth integrated. Benthic fluxes are normalized to the sediment surface and depth integrated. Air-water fluxes are normalized to the area at the surface of the lake. Stocks are calculated from concentration profiles. Negative sign stands for sinks and positive sign for sources.

Fig. 12 shows the sensitivity of the CH₄ consumption rates in June 2007 to those kinetic parameters. Iron and SO₄²⁻ dependent AOM seem to be highly sensitive to the combination of the parameters involved in the CH₄ oxidation pathways.

4. Discussion

4.1. Aerobic methane oxidation

According to measurements and model results, both aerobic and anaerobic CH₄ oxidation likely occur in the water column of Lake Pavin but are clearly spatially and seasonally dependent. As a result of the interplay of transport and biogeochemical processes, maximum rates of aerobic CH₄ oxidation are located at the transition zone between oxic and anoxic conditions, from hypoxia to anoxia (from 50 m to 62 m depth).

Maximum rates of aerobic CH₄ oxidation calculated by the model at approximately 60 m depth (1.7 x 10⁻⁶ mol L⁻¹ day⁻¹ and 9.0 x 10⁻⁷ mol L⁻¹ day⁻¹ in February and June respectively), are lower by about a factor of 10 than those expected from the experimentally derived CH₄-dependent kinetics (14 x 10⁻⁹ mol L⁻¹ day⁻¹). This is explained by the addition of an O₂-dependent term to the kinetic expression implemented in the model and, therefore, by the very low amount of O₂ available at this depth.

Finally, calculated values are in very good agreement with results reported previously within the oxycline of stratified lakes by Rudd et al. (1974) (3.8 x 10⁻⁶ mol L⁻¹ day⁻¹) and by Guérin and Abril (2007) (0.8-200 x 10⁻⁶ mmol L⁻¹ day⁻¹). Much lower aerobic rates were also observed in hypersaline lakes such as Mono Lake (Carini et al., 2005) and Big Soda Lake (Iversen et al., 1987), likely due to low methanotrophic activity as a consequence of their high salinity and pH (Zehnder and Brock, 1980; Nauhaus et al., 2002; Bastviken, 2009).

4.2. Anaerobic pathways of methane oxidation

The highest calculated rate of AOM is reported in the vicinity of 60 m depth (0.2 x 10⁻⁶ mol L⁻¹ day⁻¹) and is very close to the one measured at this depth. Rates of AOM reported by Iversen et al. (1987) and Joye et al. (1999) in the monimolimnion of Big Soda Lake (CH₄ concentration of 50 x 10⁻⁹ mol L⁻¹) and in the bottom layer of Mono Lake (CH₄ concentration of 8.4 x 10⁻⁶ mol L⁻¹), respectively, were 2-4-fold lower (48 x 10⁻⁹ mol L⁻¹ day⁻¹ and 48-85 x 10⁻⁹ mol L⁻¹ day⁻¹). In contrast, an anaerobic CH₄ oxidation rate of 3.5 x 10⁻⁶ mol L⁻¹ day⁻¹ was reported in the anoxic

Fig. 12. Simulated CH₄ consumption rates in June 2007 with estimated error bounds.
waters of the Gulf of Mexico brine pool, characterized by a lower SO$_4^{2-}$ concentration than seawater and CH$_4$ concentrations as high as in Lake Pavin (Wankel et al., 2010).

Beside published anaerobic oxidation of CH$_4$ with SO$_4^{2-}$ as electron acceptor, AOM coupled to NO$_3^-$ has been recently reported (Raghoebarsing et al., 2006; Islas-Lima et al., 2004; Modin et al., 2007). In the present study, anaerobically mediated CH$_4$ oxidation is mainly coupled to denitrification for the two time periods studied (Figs. 9 and 11).

AOM with oxides of Fe and Mn are presented in the literature as possible pathways of CH$_4$ consumption (Valentine, 2002). These reactions would provide a greater free energy yield than SO$_4^{2-}$-dependent CH$_4$ oxidation. Stimulation of potential anaerobic CH$_4$ oxidation by Mn oxides in anoxic sediments from Lake Mendota has been reported previously (Zehnder and Brock, 1980). Miura et al. (1992) suggested that, in subsols, CH$_4$ contributed to a significant proportion of Fe(III) reduction. Kumaraswamy et al. (2001) have shown a stimulation of CH$_4$ oxidation under anaerobic conditions when Fe(III) was added to anoxic rice soil samples. More recently, Crowe et al. (2010) suggested that anaerobic CH$_4$ oxidation could likely be coupled to the reduction of Fe (and/or Mn) (hydr)oxides in the water column of Lake Matano, the world’s largest known ferruginous basin. From the latter study, a rate of AOM of $5 \times 10^{-2}$ mol L$^{-1}$ day$^{-1}$ was estimated. It is 10 times higher than the maximum rate estimated for Fe-AOM in this work. The latter is also several times lower than the rates measured within marine sediments by Beal et al. (2009). Finally, although higher concentrations of particulate Fe are encountered in Lake Pavin compared with those in Lake Matano, denitrification seems to be the preferential CH$_4$ consumption pathway, followed by Fe, SO$_4^{2-}$ and Mn reductions in order of decreasing importance.

Many studies have reported AOM in freshwater and/or seawater sediments. By far, the fewest have measured AOM occurring in anoxic water columns and the rates reported are generally lower than rates observed for sediments, primarily because microbial density is substantially higher in sediments. Although, there is no direct evidence for those alternative consumption pathways (Fe/Mn-AOM) in Lake Pavin, the model suggests that Fe-dependent CH$_4$ oxidation may occur in the water column (Fig. 11). These findings are in good agreement with preliminary results of incubations of Lake Pavin water samples from 70 m depth, with Fe oxides shown that CH$_4$ may be used as electron donor for Fe reduction (Lehours, 2006).

### 4.3. Sources and sinks of methane in Lake Pavin

In February 2007, during the winter mixing period, and to a lesser extent in June 2007, aerobic and anaerobic CH$_4$ oxidation normalized to the whole water column clearly appear as the major sink for CH$_4$ (Table 5). Utsumi et al. (1998) and Guérin and Abril (2007) showed that CH$_4$ oxidation in the water column was the dominant CH$_4$ sink, removing respectively 94% of CH$_4$ during the overturn period of Lake Nojiri and 90% of CH$_4$, on average, through-out the year in the Petit Saut reservoir.

The flux of CH$_4$ to the atmosphere estimated in February 2007 ($0.2 \times 10^{-3}$ mol m$^{-2}$ day$^{-1}$) appears to be lower than the global average flux from lakes: 2.69 (1.06–5.6) $\times$ 10$^{-3}$ mol m$^{-2}$ day$^{-1}$ (Aselmann and Crutzen, 1989). The Lake Pavin flux is closer to the one of lake 227 reported in Rudd and Hamilton (1978) ($0.34 \times 10^{-3}$ mol m$^{-2}$ day$^{-1}$) or those found at Big Soda Lake ($0.036 \times 10^{-3}$ mol m$^{-2}$ day$^{-1}$; Iversen et al., 1987) or at Mono Lake ($0.312 \times 10^{-3}$ mol m$^{-2}$ day$^{-1}$; Joyce et al., 1999). In June 2007, CH$_4$ flux, although reversed, remains within calculation uncertainties and can be compared to the situation of Lake Baikal where CH$_4$ flux was not significantly different from zero (Schmid et al., 2007). Once normalized to the whole lake surface, air–water exchange is not an important sink or source of CH$_4$ for the two time periods studied (Table 5).

Although methanogenesis occurs in the anoxic water layers, CH$_4$ concentration in Lake Pavin is mainly due to CH$_4$ flux from the sediment. Methane fluxes from sediments calculated from this study are in good agreement with those reported by Iversen et al. (1987) in Big Soda Lake ($2.9 \times 10^{-3}$ mol m$^{-2}$ day$^{-1}$).

Maximum methanogenic rates of $5 \times 10^{-8}$ mol L$^{-1}$ day$^{-1}$ were calculated at 90 m depth. Winfrey and Zeikus (1979) and Iversen et al. (1987) also reported water column CH$_4$ production with maximum rates of $1.2 \times 10^{-6}$ mol L$^{-1}$ day$^{-1}$ at Knaack Lake and 10.5 $\times$ 10$^{-8}$ mol L$^{-1}$ day$^{-1}$ at Big Soda Lake, respectively. According to Winfrey and Zeikus (1979), the existence of a permanent anaerobic habitat enables methanogenic Archaea to establish themselves in the anaerobic waters and actively produce CH$_4$. Additionally, the water chemistry in meromictic lakes is also an important factor in determining whether methanogenesis occurs in the water column or in the sediment. The absence of SO$_4^{2-}$ and NO$_3^-$ in the bottom waters of Lake Pavin enables methanogenesis. Calculations demonstrate that CH$_4$ produced in the water column results mainly from the degradation of dissolved organic C. In the model, it is assumed that DOC is highly biodegradable. According to Pourriot and Meebeek (1995) the organic matter resulting from phytoplankton lysis presents a high fraction of biodegradable organic C (>80% of DOC).

Interestingly, in the upper layers of the mixolimnion (from the surface to approximately 12 m), significantly higher CH$_4$ concentrations were measured in June and September 2006 than those from lower layers (from 12 m to 55 m), suggesting CH$_4$ generation in the photic zone (Fig. 4b). Liu et al. (1996) also reported higher CH$_4$ concentrations in surface water of the highly productive Lake Lugano. These CH$_4$ maxima in the oxic surface layers of lakes may correspond to the presence of anaerobic microhabitats in particular organic matter (Karl and Tilbrook, 1994), and/or aerobic CH$_4$ production through alternative pathways, analog to methylphosphonate decomposition recently evidenced in the ocean (Karl et al., 2008).

An alternative explanation for the higher CH$_4$ content in surface layers than in the middle layers is proposed by Bastviken et al. (2008): the enrichment may be due to CH$_4$ diffusion from epilimnetic sediment combined with higher water turbulence in the surface layer.

In June 2007, CH$_4$ sinks counterbalance sources and participate in maintaining the observed steady state in Lake Pavin (Table 5). In February 2007, the magnitude of the sinks is about twice as large as the sources. However, when compared to the whole stock of CH$_4$, seasonal variations in CH$_4$ sinks are clearly smoothed on the yearly scale. One can also calculate an average biogeochemical renewal time (stock/sinks) ranging from 12 to 30 years for CH$_4$. The stock of CH$_4$ is essentially located in the monimolimnion which has a water residence time of 70 years (Assayag et al., 2008). This stresses the importance of biogeochemical processes as main drivers of CH$_4$ control in Lake Pavin.

### 5. Conclusions

A biogeochemical model was developed and applied to data from Lake Pavin in order to assess the most significant pathways of CH$_4$ consumption in this lake. For instance, aerobic and anaerobic oxidation of CH$_4$ both occur in the water column of Lake Pavin, with aerobic oxidation being the dominant pathway. The highest rate of anaerobic oxidation of CH$_4$ is observed at approximately 60 m depth where NO$_3^-$ is the main electron acceptor involved. Iron dependent anaerobic CH$_4$ oxidation may occur in the water column but remains a minor pathway. Methane oxidation rates seem to be sensitive to vertical mixing and to the combination of all the
kinetic parameters of the CH₄ consumption pathways. The main source of CH₄ is always associated with the benthic flux with little water column methanogenesis, while CH₄ sinks are more variable. Methane oxidation is the main sink and CH₄ evasion through water-atmosphere exchange corresponds to less than 10% of the biogeochemical sinks. This detailed study also shows that interpretation of CH₄ monitoring in Lake Pavin has to consider the interannual and decadal time scales.

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